

# Experimental observation of localized structures in medium size VCSELs

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**Abstract:** We report experimental evidence of spontaneous formation of localized structures in a 80 $\mu$ m diameter Vertical-Cavity Surface-Emitting Laser (VCSEL) biased above the lasing threshold and under optical injection. Such localized structures are bistable with the injected beam power and the VCSEL current. We experimentally investigate the formation of localized structures for different detunings between the injected beam and the VCSEL, and different injection beam waists.

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## 1. Introduction

The emergence of localized structures (LSs) in out of equilibrium systems has witnessed tremendous progress in the last years (see recent overviews [1–6]). They have been found in many different areas of science, such as nonlinear optics [4–6], chemistry [7–13], ecology [14–17], or in mathematical models [18–20]. In optics, they are called cavity solitons and they are potentially interesting for all-optical control of light, optical storage, and information processing. Cavity solitons are stationary localized structures appearing on the homogeneous

background of the field emitted by a nonlinear microresonator with a high Fresnel number. Early reports on cavity solitons were provided in [21, 22]. They described numerical simulations of pulse propagation in bistable systems. Later on, it was shown that the existence of LSs does not require a bistable homogeneous steady state [23, 24]. Their existence requires a multistable regime, i.e. a coexistence of a homogeneous steady state and periodic structures. This condition can be realized under the injection of a stationary wave called holding beam. Localized structures can be spatially independent and randomly distributed [23, 24]. When LSs are brought in proximity of one another they start to interact via their oscillating, exponentially decaying tails. This interaction leads to clustering phenomena [25].

A vast amount of experimental work has been realized on localized structures. They have been observed in photorefractive materials [26], in liquid crystal valves [27–29], in lasers with saturable absorbers [30], in degenerate optical parametric mixing [31], in photorefractive oscillators with saturable absorber [32], in spin  $\frac{1}{2}$  atomic systems with optical feedback [33, 34], and in Kerr media [35]. They have been predicted to exist in lasers with saturable absorbers [36], in left-handed materials [37] and in VCSELs [38, 39]. They have been experimentally demonstrated in driven passive microcavities [40], amplifier [41, 42] and optically injected lasers [43, 44]. Nowadays, localized structures in VCSELs is an active field in nonlinear optics [3, 4, 45] due to the maturity of the semiconductor technology and the possible applications of CSs as, e.g. all optical delay lines [46], logic gates [47], and microscope [48]. Moreover, the fast response time of VCSELs makes them attractive materials for potential applications towards all-optical control of light.

Various mechanisms have been proposed to generate localized structures in VCSELs. Experimental evidence of LSs has been performed by using two beams: a holding beam and a writing beam [41]. The holding beam allows to ensure optical bistability and the writing beam is used to locally make the system evolve from the lower branch of the bistability to the higher and reciprocally. Soon later it has been shown that LSs could be observed in absence of driving (holding) beam. In this case, LSs have been realized on three different experimental schemes: a monolithic VCSEL with a saturable absorber [49], two coupled VCSELs in a face-to-face configuration [50], and a VCSEL with frequency selective feedback with [51] or without [52] a writing beam. LSs are not necessary stationary objects: it has been shown theoretically that they can exhibit a spontaneous motion under the thermal effects [53, 54], or by a regular delayed feedback [55–59]. If the pump has a circular profile the LS moves along the boundary under the presence of a saturable absorber [60]. This motion is a consequence of the drift instability described in [36].

Localized structures are likely to appear even without the adjunction of a writing beam. To our knowledge, reports on experimental observation of LSs in an optically injected VCSEL have so far been limited to broad area (wider than  $100\mu\text{m}$ ) VCSELs [41, 42, 61, 62]. Using injection orthogonally polarized to the dominant polarization, a LS was observed in a  $40\mu\text{m}$  diameter device [63], but only one and placed exactly in the center, indicating that the symmetry of the boundaries might be important. The influence of boundary conditions on the stability and existence of LSs will be investigated in near future. In this paper, we demonstrate LS and clusters of LSs in a  $80\mu\text{m}$  diameter device. The paper is organized as follows: in section 2, we describe the experimental setup and we characterize the solitary and optically injected VCSEL. In section 3, we describe the spontaneous formation of localized structures for different waists of the injection beam, different frequency detunings with respect to the VCSEL and different injection currents. Finally, in section 4, we conclude.

## 2. Experimental setup and VCSEL characteristics

### 2.1. Description of the experimental setup

The experimental setup used for the generation of two-dimensional localized structures is shown in Fig. 1. The setup contains three main parts. (i) Injection: the holding beam is provided by a commercial Sacher Lasertechnik TEC100-0960-60 External Cavity Diode Laser (Master) isolated with OFR IO5-TiS2-HP optical isolator (OI). The long term electrical and temperature stability of this laser are less than 20 mA RMS and 0.05°C, respectively. The wavelength (frequency) sensitivity is 0,695 nm par 100V with piezo actuator. Due to the power limitation of the tunable injection laser, we do not implement a writing beam. A half wave plate ( $\lambda/2$ ) is used to tune the linear polarization. The injection beam power is tuned using a variable optical density filter (VODF). The detuning between the master laser and the VCSEL is defined as  $\theta = \nu_{inj} - \nu_{slave}$ , where  $\nu_{inj}$  is the frequency of the injection beam, and  $\nu_{slave}$  the frequency of the strongest peak in the spectrum of the standalone VCSEL. It is experimentally tuned by changing the wavelength of the injection beam. The beam waist is defined as the diameter of the smallest circle in the plane of propagation of the injection beam containing half of the beam power when it encounters the VCSEL. The beam waists used in our measurements are 100 $\mu$ m and 50 $\mu$ m. The power of the source is monitored by a Newport 818-SL photodiode connected to a Newport 2832-C powermeter. This system yields about 100 Hz data acquisition and transfer rate. This photodiode is indicated PD<sub>1</sub> in Fig. 1. (ii) Nonlinear material: we use a 80 $\mu$ m diameter, bottom emitting InGaAs multiple quantum well VCSEL [64], which has a threshold current of 42.5 mA at 25.0°C. The response time scale involved in the space-time dynamics of the material ( $\approx$ ps) and carriers ( $\approx$ ns) are much faster than the thermal time scale ( $\approx$   $\mu$ s). (iii) Detection of the VCSEL output: the field emitted by the VCSEL is analyzed using an ANDO AQ6317-B optical spectrum analyzer (OSA). This device has a resolution of 0.02nm at 980nm. A CCD camera is used to monitor the near field output profile of the VCSEL. For detection of the output VCSEL power we use the photodiode PD<sub>2</sub>, which is identical to the photodiode PD<sub>1</sub>.

### 2.2. VCSEL characteristics

Measurements of the VCSEL optical spectrum and the near field profile as a function of current and optical injection power are performed. The standalone device is studied as well.

To characterise the standalone VCSEL, we first measure its optical spectrum as a function of current. The optical spectra of the solitary VCSEL as a function of injected current in vertical and horizontal polarization directions are depicted in Fig. 2. In the vertical polarization optical spectrum, the threshold current and the current-induced thermal red shift are indicated with solid white lines as shown in Fig. 2(a). From these optical spectra, we see that the power is mostly emitted along the vertical polarization direction. However, in the horizontal polarization optical spectrum there is no visible threshold, as shown in Fig. 2(b). Therefore, close to threshold, the VCSEL emits linearly polarized light.

The near field emission profile of the VCSEL is shown in Fig. 3(a). This measurement has been obtained for  $I = 45.0\text{mA} > I_{th} = 42.0\text{mA}$ , where  $I_{th}$  is the lasing threshold at 25°C. The corresponding optical spectrum is plotted in Fig. 3(b). These measurements have been performed at a constant temperature of  $T_{sub} = 25.0^\circ\text{C}$ . The near field image in Fig. 3(a) shows circular standing-wave patterns along the perimeter, sometimes referred to as flower-like, or daisy mode [65]. It reminds of the one observed in smaller area VCSELs [63]. The spectrum, depicted in Fig. 3(b), contains two relatively closely spaced wavelengths, i.e. the pattern is not a single transverse mode.

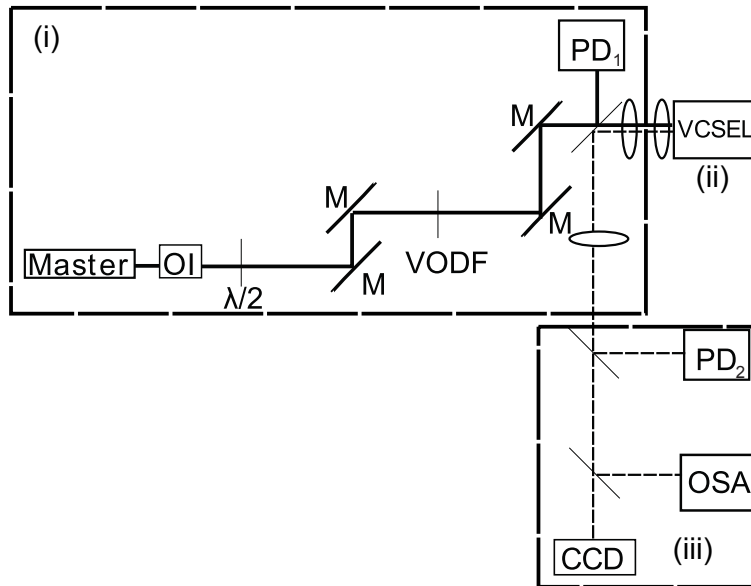


Fig. 1. Experimental setup schematic. The full line is the path of the light from the master laser, whereas the dashed line is the path followed by the light from the VCSEL. (i): injection preparation and monitoring; Master: master laser, OI: optical isolator,  $\lambda/2$ : half wave plate, M: mirror, VODF: variable optical density filter (ii): VCSEL; (iii): analysis branch; PD: photodiode, OSA: optical spectrum analyser.

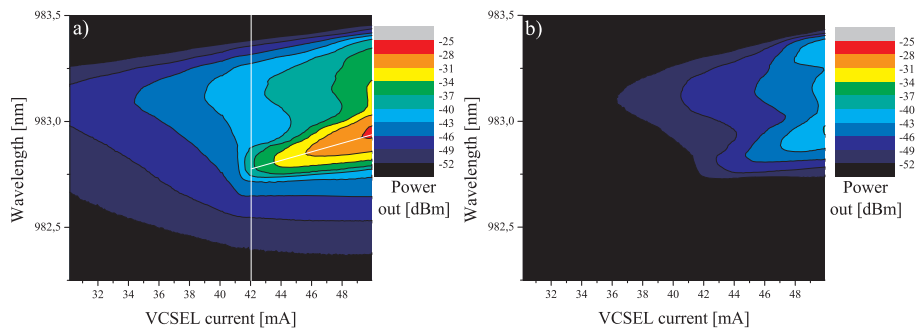


Fig. 2. Optical spectra of the solitary VCSEL as a function of pump current; (a): vertical polarization, (b): horizontal polarization. On part (a), the lasing threshold and current induced thermal red shift have been evidenced by solid white lines. Both measures have been performed with the VCSEL kept at  $T_{sub} = 25.0^\circ\text{C}$ .



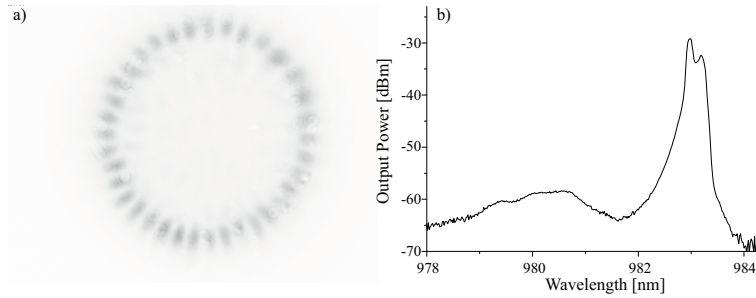


Fig. 3. Solitary VCSEL characteristics obtained for  $I = 45.0\text{mA}$  and  $T_{sub} = 25.0^\circ\text{C}$ . (a) near field profile in the transverse plane. Black corresponds to high optical power whereas white corresponds to low optical power. (b) is the corresponding optical spectrum.

### 2.3. Optically injected VCSEL

Finally, we examine the spectrum of the VCSEL submitted to optical injection with a polarization direction parallel to the one of the VCSEL. We set the VCSEL current at  $I = 45.0\text{mA}$  and we keep the substrate temperature constant at  $T_{sub} = 25.0^\circ\text{C}$ . Injection locking requires high enough injected power as well as a negative and small enough frequency detuning [66]. For this purpose, we need an injection wavelength greater than  $982.91\text{nm}$ . The measurement of the optical spectra is shown in Fig. 4. These spectra have been measured for two values of the injected power determined by the photodiode PD<sub>1</sub>. When the injection beam power is  $P_{inj} = 850\mu\text{W}$ , the VCSEL is frequency pulled towards the master laser frequency which is indicated by a short vertical arrow, as shown in Fig. 4(a). The near field emission profile changes, even if the flower-like mode has not disappeared from the emitting surface of the VCSEL. In this case, there is no injection locking of the VCSEL. However, for an injection power of  $P_{inj} = 2.04\text{ mW}$ , the VCSEL is locked to the master laser as shown in Fig. 4(b).

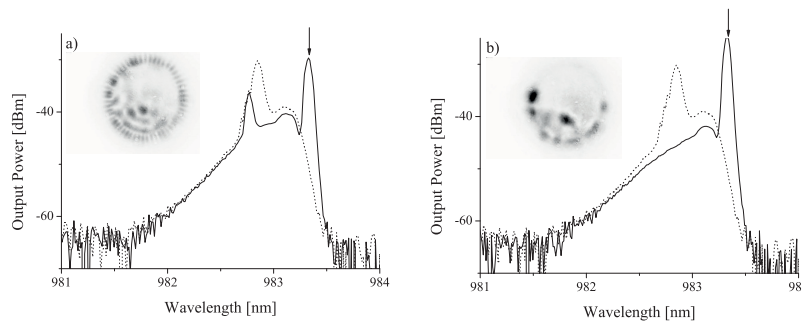


Fig. 4. Dashed lines: optical spectra of the free running VCSEL obtained for  $I = 45.0\text{mA}$  and  $T_{sub} = 25.0^\circ\text{C}$ . Solid lines: optically injected VCSEL with  $\lambda_{inj} = 983.24\text{nm}$  (indicated by a vertical arrow) and injection power of (a)  $P_{inj} = 850\mu\text{W}$  and (b)  $P_{inj} = 2.04\text{ mW}$ . The insets are near field images of the optically injected VCSEL.

## 3. Spontaneous formation of localized structures in an optically injected VCSEL

After the characterization of the VCSEL, we investigate the formation of two-dimensional localized structures in two different regimes. Our experimental setup possesses three control parameters, namely the injected power, frequency detuning, and the VCSEL current. This setup

may then undergo a bistable behavior when either varying the injected beam power or the VCSEL current. In addition, we study the formation of 2-dimensional LSs for different values of detuning and also for different beam waists. All experimental measurements have been performed when the VCSEL operated in an injection locked regime as in Fig. 4(b).

We first investigated LSs bistable with the injection power for a fixed value of the detuning parameter  $\theta = -174$  GHz and for a fixed value of the injection beam waist  $100\mu\text{m}$ . The experimental results are summarized in the bistable curve in Fig. 5(a). The VCSEL output power as a function of the injected beam power, which is shown in this figure undergoes a bistable behavior between a single LS (i) and a two LSs (ii) states, as shown in Fig. 5(a). The experimental procedure to obtain LSs consists of increasing the injection power, and, just as the locking region is reached, a single LS appears. Then, as we further increase the optical injection power by tuning the variable optical density filter (VODF), we observe transition from a single LS state towards a two-LSs state. This behavior corresponds to a spontaneous switching on. To realize the switching off, we decrease the injection power. The two LSs persist until the system reaches the switching down point, over which the system relaxes to the single peak state. The density plot of both 1-LS and 2-LSs near field are recorded by using a CCD camera. Cross sections of the single and the two-LSs states near-field are shown in Figs. 5(b) and 5(c). A similar behavior of switching on and off has been observed while the detuning parameter was  $\theta = -157$ GHz and the beam waist  $100\mu\text{m}$ . A fundamental characteristic of LSs is that it has

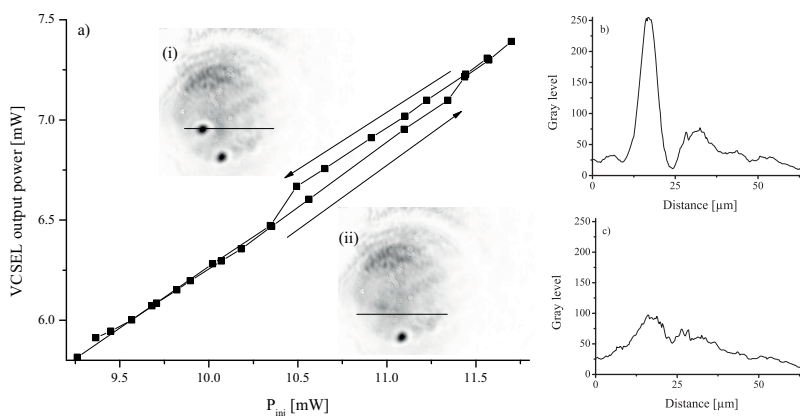


Fig. 5. Bistability between one and two-peaked LSs inside the near field of the VCSEL as a function of the optical injection power. (a): power emitted by the VCSEL as a function of the optical injection power for  $\theta = -174$ GHz and a beam waist of  $100\mu\text{m}$ . The insets (i) and (ii) respectively represent near field profile on the higher and lower branch of the hysteresis. (b) and (c): one dimensional profile along the horizontal line drawn on the aforementioned insets.

an oscillatory tail, which decays exponentially with the distance to the center of the LS. This behavior has been shown experimentally with other optical systems [34, 35, 67]. We recover this fundamental property in VCSELs. An example of such a behavior is illustrated in Fig. 6.

In order to increase the optical power on the VCSEL, we decreased the beam waist to  $50\mu\text{m}$  and the detuning to  $\theta = -118$ GHz. We could then reach a multipiece regime as shown in Fig. 7(a). In this case, three states can exist, with a bound state of two LSs (2P), this bound state accompanied with a single peak localized structure (3P), or a four-peak LS (4P). Cross sections along the vertical lines in the insets Fig. 7 (2P), (3P) and (4P) correspond to the aforementioned states. A bistable behavior has also been observed while the detuning was  $\theta = -146$ GHz.

Finally, a bistable behavior between two states is observed when varying the VCSEL current.



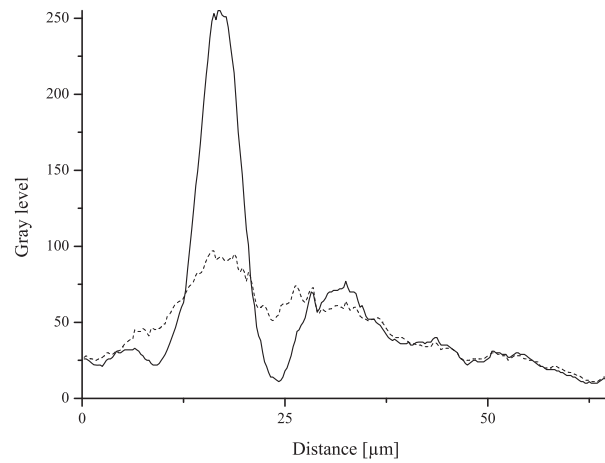


Fig. 6. Cross sections along the solid lines indicated in Fig. 5(a), (i) and (ii). The dashed line is the state (ii)(lower branch of the hysteresis), whereas the full line is the system with a LS (upper branch of the hysteresis).

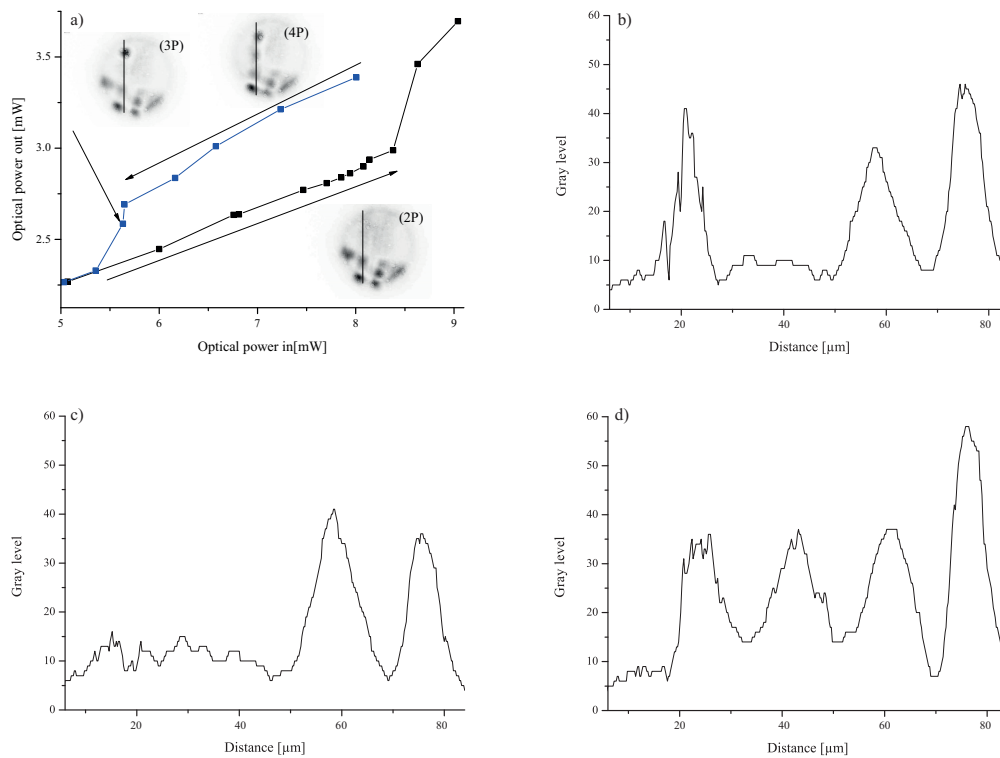


Fig. 7. Bistability between three states inside the near field of the VCSEL as a function of the optical injection power. (a): power emitted by the VCSEL as a function of the optical injection power for  $\theta = -118\text{GHz}$  and  $50\mu\text{m}$  injection beam waist. The insets (2P) and (3P) and (4P) represent near field profile of the three possible states of the system. (b), (c) and (d): one dimensional profile along the vertical line drawn on the aforementioned insets.

We set the beam waist at  $100\mu\text{m}$  and the optical injection power at  $17\text{mW}$ . When varying the VCSEL current, we observe bistability of a LS. An example of such a behavior is illustrated in Fig. 8(a). Cross sections along the vertical lines in Figs. 8(b) and 8(c) correspond to the near field profile of the insets (i) and (ii), respectively.

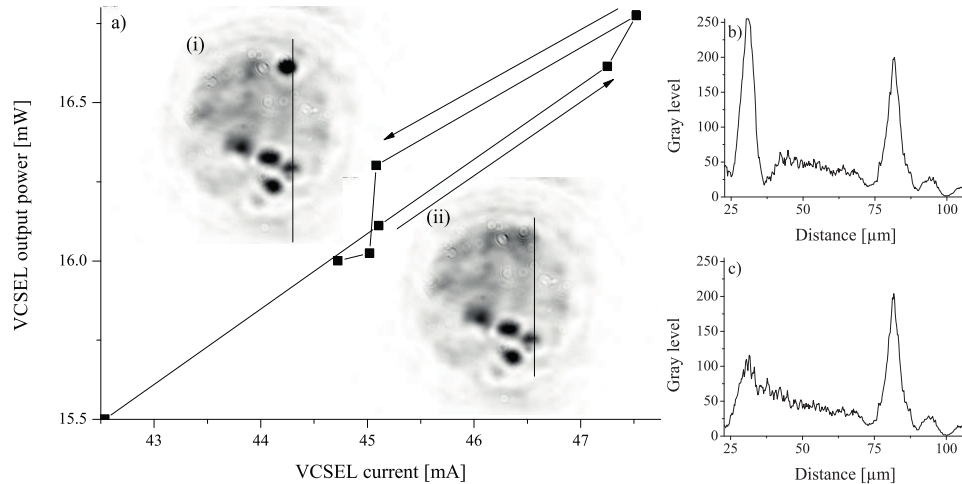


Fig. 8. Bistability between two states inside the near field of the VCSEL as a function of the VCSEL current. (a): power emitted by the VCSEL as a function of the VCSEL current for  $100\mu\text{m}$  and  $17\text{mW}$  optical injection beam waist and power, respectively. The bistable region of the curve has its detuning  $\theta$  varying between  $-185\text{GHz}$  and  $-166\text{GHz}$  due to the current induced thermal red shift. The insets (i) and (ii) represent near field profile of the two possible states of the system. (b) and (c): one dimensional profile along the vertical line drawn on the aforementioned insets.

#### 4. Conclusions and perspectives

To conclude, we report experimental evidence of spontaneous formation of spatially localized structures in a  $80\mu\text{m}$  diameter VCSEL submitted to optical injection. Different detunings between the frequencies of the injection beam and the VCSEL have been investigated, as well as different beam waists. This behavior occurs in two different bistability regimes by varying either the optical injection power or the VCSEL current.

In future work, we plan to investigate experimentally the role of delay feedback, and establish a link with our predictions on a full rate equation model of broad area VCSELs [56, 57, 59] subject to simultaneous time-delayed feedback and optical injection. This study showed that the modulation instability region strongly depends on both the feedback strength and the feedback phase. Furthermore, the optical feedback induces traveling wave instabilities in the system, as well as spontaneous motion with a constant velocity of a single peak LS.

The analysis of local polarization dynamics [63] in the transverse plane of the resonator, the occurrence of polarization patterns and possibility the realization of LSs between two polarization modes can be of interest as well. Studies of vector solitons in polarization will be theoretically carried out using the spin-flip model of VCSELs, and implemented experimentally.

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